

# Introduction to the Revised Mathematics TEKS 

SIDE-BY-SIDE TEKS COMPARISON GRADE 3

TEXAS EDUCATION AGENCY

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Grade 3 - Mathematics
(a) Introduction.
(1) Within a well-balanced mathematics curriculum, the primary focal points at Grade 3 are multiplying and dividing whole numbers connecting fraction symbols to fractional quantities, and standardizing language and procedures in geometry and measurement.
(a) Introduction
(1) The desire to achieve educational excellence is the driving force behind the Texas essential knowledge and skills for mathematics, guided by the college and career readiness standards. By embedding statistics, probability, and finance, while focusing on computational thinking, mathematical fluency, and solid understanding, Texas will lead the way in mathematics education and prepare all Texas students for the challenges they will face in the 21st century.
(a) Introduction.
(4) The primary focal areas in Grade 3 are place value, operations of whole numbers, and understanding fractional units. These focal areas are supported throughout the mathematical strands of number and operations, algebraic reasoning, geometry and measurement, and data analysis. In Grades 3-5 the number set is limited to positive rational numbers. In number and operations, students will focus on applying place value, comparing and ordering whole numbers, connecting multiplication and division, and understanding and representing fractions as numbers and equivalent fractions. In algebraic reasoning, students will use multiple representations of problem situations, determine missing values in number sentences, and represent real-world relationships using number pairs in a table and verbal descriptions. In geometry and measurement, students will identify and classify two-dimensional figures according o common attributes, decompose composite figures formed by rectangles to determine area, determine the perimeter of polygons, solve problems involving time, and measure liquid volume (capacity) or weight. In data analysis, students will represent and interpret data.

The definition of a well-balanced mathematic curriculum has expanded to include the CCRS. A focus on mathematical fluency and solid understanding allows for rich exploration of the primary focal points.

## The 2012 paragraph that highlights more

 specifics about grade 3 mathematics content follows paragraphs about the mathematical process standards and mathematical fluency. This supports the notion that the TEKS are expected to be learned in a way that integrates the mathematical process standards to develop fluency.The 2012 paragraph has been updated to align to the 2012 grade 3 mathematics TEKS.

The 2012 paragraph highlights focal areas or topics that receive emphasis in this grade level. These are different from focal points which are part of the Texas Response to Curriculum Focal Points [TXRCFP]. "[A] curriculum focal point is not a single TEKS statement; a curriculum focal point is a mathematical idea or theme that is developed through appropriate arrangements of TEKS statements at that grade level that lead into a connected grouping of TEKS at the next grade level" (TEA, 2010, p. 5).

The focal areas are found within the foca points. The focal points may represent a subset of a focal area, or a focal area may represent a subset of a focal point. The focal points within the TXRCFP list related grade-
Old TEKS $\quad$ Current TEKS (2012) Supporting Information
(a) Introduction.
(3) Throughout mathematics in Grades 3-5 students develop numerical fluency with conceptual understand and computational accuracy. Students in Grades 3-5 use knowledge of the base-ten place value system to compose and decompose numbers in order to solve problems requiring precision, estimation, and reasonableness. By the end of Grade 5, students know basic addition, subtraction, multiplication, and division, subts and are using them to work flexibly, efficiently, and accurately with flexibly, efficiently, and accurately with
numbers during addition, subtraction, multiplication, and division computation.
(a) Introduction.
(3) For students to become fluent in mathematics students must develop a robust sense of number. The National Research Council's report, "Adding It Up," defines procedural fluency as "skill in carrying out procedures flexibly, accurately, efficiently and appropriately." As students develop procedural fluency, they must also realize that true problem solving may take time, effort, and perseverance. Students in Grade 3 are expected to perform their work without the use of calculators.

The Revised TEKS (2012) include the use of the words "automaticity," "fluency"/"fluently," and "proficiency" with references to standard algorithms. Attention is being given to these descriptors to indicate benchmark levels of skill to inform intervention efforts at each grade level. These benchmark levels are aligned to national recommendations for the development of algebra readiness for enrollment in Algebra I.

Automaticity refers to the rapid recall of facts and vocabulary. For example, we would expect a fifth-grade student to recall rapidly the sum of 5 and 3 or to identify rapidly a closed figure with 3 sides and 3 angles.
o be mathematically proficient, student must develop conceptual understanding, procedural fluency, strategic competence, adaptive reasoning, and productive
disposition (National Research Council, 2001,
p. 116).
"Procedural fluency refers to knowledge of procedures, knowledge of when and how to use them appropriately, and skill in
performing them flexibly, accurately, and
efficiently" (National Research Council, 2001,
p. 121).
"Students need to see that procedures can be developed that will solve entire classes of problems, not just individual problems"
National Research Council, 2001, p. 121).

Procedural fluency and conceptua
(a) Introduction.
(4) Problem solving, language and communication, connections within and outside mathematics, and formal and informal reasoning underlie all content areas in mathematics. Throughout mathematics in Grades 3-5, students use these processes together with technology and other mathematical tools such as manipulative materials to develop conceptual understanding and solve problems as they do mathematics.
(a) Introduction.
(2) The process standards describe ways in which students are expected to engag in the content. The placement of the process skill at the beginning of the draft is intentional. The process skills weave the other knowledge and skills together so that students may be successful problems solvers and use mathematics efficiently and effectively in daily life. The process standards are integrated at every grade level and course. When possible, students will apply mathematics to problems arising in everyday life, society, and the workplace. Students will use a problemsolving model that incorporates analyzing given information, formulating a plan or strategy, determining a solution, justifying the solution, and evaluating the problemsolving process and the reasonableness of the solution. Students will select
appropriate tools such as real objects, manipulatives, algorithms, paper and pencil, and technology and techniques uch as mental math, estimation, numb ense, and generalization and abstraction n and abstraction o solve problems. Students will effectively communicate mathematical ideas, reasoning, and their implications using multiple representations such as symbols, diagrams, graphs, computer programs, and language. Students wil analyze mathematical relationships to connect and communicate mathematical ideas. Students will display, explain, or ustify mathematical ideas and arguments using precise mathematical language in written or oral communication
(a) Introduction.
5) Statements that contain the word
"including" reference content that must be mastered, while those containing the phrase "such as" are intended as possible

The State Board of Education approved the retention of some "such as" statements within the TEKS where needed for clarification of content.

This 2012 paragraph occurs second in the Revised TEKS (2012) instead of fourth as in the current TEKS. This highlights the continued emphasis on process skills that now continue from Kindergarten through high school mathematics.

The language of this 2012 introductory paragraph is very similar to the Mathematical Process Standard strand within the Revised TEKS (2012).

This 2012 introductory paragraph includes generalization and abstraction with the text from (1)(C)

This 2012 introductory paragraph includes computer programs with the text from (1)(D)

This 2012 introductory paragraph states students will use mathematical relationships to generate solutions and make connections and predictions." instead of the text from (1)(E).

Grade 3 - Mathematics

3(1)(A) Number, operation, and quantitative reasoning. The student uses place value to communicate about increasingly large whole numbers in verbal

-     + 

and written form, including money.
The student is expected to use place value to read, write (in symbols and words), and describe the value of whole numbers through 999,999.

## $3(1)(B)$ Number, operation, and

 quantitative reasoning. The student uses place value to communicate about$+\quad$ increasingly large whole numbers in verba and written form, including money.

The student is expected to use place value to compare and order whole numbers through 9,999.

3(1)(C) Number, operation, and quantitative reasoning. The student uses place value to communicate about
O place value to communicate about and written form, including money.
The student is expected to determine the value of a collection of coins and bills.

## $3(2)(A)$ Number, operation, and

 quantitative reasoning. The student uses fraction names and symbols (with+ denominators of 12 or less) to describe fractional parts of whole objects or sets of objects.

The student is expected to construct concrete models of fractions.

## 3(2)(A) Number and operations.The

 student applies mathematical process standards to represent and compare whole numbers and understand relationships related to place value.The student is expected to compose and decompose numbers to 100,000 as a sum of so many ten thousands, so many thousands, so many hundreds, so many tens, and so many ones using objects, pictorial models, and numbers, including expanded notation as appropriate.

3(2)(D) Number and operations.Th student applies mathematical process standards to represent and compare whole numbers and understand relationships related to place value.

The student is expected to compare and order whole numbers up to $\mathbf{1 0 0}, 000$ and represent comparisons using the
symbols $>,<$, or $=$.
$3(4)(C)$ Number and operations.The student applies mathematical process standards to develop and use strategies and methods for whole number computations in order to solve problems with efficiency and accuracy.

The student is expected to determine the value of a collection of coins and bills.

## 3(3)(A) Number and operations.The

 student applies mathematical process standards to represent and explain fractional units.The student is expected to represent fractions greater than zero and less than or equal to one with denominators of 2, 3, 4,6 , and 8 using concrete objects and pictorial models, including strip diagrams and number lines.

Specificity has been added as to how students are expected to read, write, and describe the value of whole numbers, including expanded notation as appropriate.

Composing and decomposing whole numbers may focus on place value such as the relationship between standard notation and expanded notation. It may also include decomposing 787 into the sum of 500, 200, 50,30 , and 7 to prepare for work with compatible numbers when adding whole numbers with fluency.
Students are expected to represent whole numbers to 100,000 with objects and pictorial models.
With the revised SE, students are not
expected to address numbers between 100,000 and $1,000,000$ as with the current SE.
Specificity regarding notation has been
included with the inclusion of the symbols $>$, $<$, or $=$.

The revised SE expects students to also compare and order whole numbers between 9,999 and 100,000 in addition to whole numbers through 9,999.

The revised SE is the same as the current SE.
The knowledge and skills statement clarifies that the focus is whole number computations so students are expected to determine the collection of coins in cents.

Specificity has been added for the fractions that students are expected to model.
Fractions are greater than zero and less than or equal to one. The denominators may be 2
$3,4,6$, or 8 . Concrete models should be
linear in nature to build to the use of strip diagrams and number lines.
Students are expected to represent fractions using pictorial models, including strip diagrams and number lines.

## Grade 3 - Mathematics

Old TEKS: Number, Operation, and
Old TEKS: Number, Ope
Supporting I nformation

3(2)(B) Number, operation, and quantitative reasoning. The student uses fraction names and symbols (with denominators of 12 or less) to describe fractional parts of whole objects or sets of + objects

The student is expected to compare fractional parts of whole objects or sets of objects in a problem situation using concrete models.

3(3)(H) Number and operations.The student applies mathematical process standards to represent and explain fractional units.

The student is expected to compare two fractions having the same numerator or denominator in problems by reasoning bout their sizes and justifying the conclusion using symbols, words objects, and pictorial models.
$3(2)(C)$ Number, operation, and quantitative reasoning. The student uses fraction names and symbols (with

+ denominators of 12 or less) to describe fractional parts of whole objects or sets of objects.

The student is expected to use fraction names and symbols to describe fractional parts of whole objects or sets of objects.

## (3)(C) Number and operations.The

 student applies mathematical process standards to represent and explain fractional units.The student is expected to explain that the unit fraction $\mathbf{1 / b}$ represents the quantity formed by one part of a whole that has been partitioned into $b$ equal parts where $b$ is a non-zero whole number.

3(3)(D) Number and operations. The student applies mathematical process standards to represent and explain fractional units.

The student is expected to compose and decompose a fraction $\mathbf{a} / \mathbf{b}$ with a numerator greater than zero and less than or equal to $b$ as a sum of parts $1 / b$.

The revised SE adds specificity to the number of fractions a student compares. It also adds specificity to the types of fractions being specificity to the tractions having the same numerator or denominator.

Fractions should have denominators of 2, 3, 4,6 , or 8.

Examples include situations such as comparing the size of one piece when sharing a candy bar equally among four people or equally among three people

Students justify conclusions using objects
Students justify conclusions about their comparisons using symbols, words, and pictorial models.

The current SE was separated into three revised SEs. Revised SE 3(3)(C) focuses on unit fractions.

Specificity has been added to the descriptions students are expected to provide with symbols for writing fractions.

Fractions should have denominators of 2, 3, 4, 6, or 8 .

Students are expected to describe or explain the fraction $1 / b$ as the quantity formed by one part of a whole that has been partitioned into $b$ equal parts where $b$ is a non-zero whole number.

A fraction may a part of a whole object or part of a set of objects.
The current SE was separated into three revised SEs. Revised SE 3(3)(D) focuses on non-unit fractions.

Fractions should have denominators of 2, 3, 4, 6, or 8 .

Specificity has been added as to how students are expected to describe fractional parts of whole objects. Students are expected to compose and decompose fractions. For example, $3 / 8=1 / 8+1 / 8+1 / 8$.

A fraction may be a part of a whole object or part of a set of objects to build to $3(3)(\mathrm{E})$.

## Grade 3 - Mathematics

| OId TEKS: Number, Operation, and <br> Quantitatifve Reasoning | Current TEKS (2012) |
| :--- | :--- |
| 3(2)(C) Number, operation, and <br> quantitative reasoning. The student uses <br> fraction names and symbols (with <br> denominators of 12 or less) to describe <br> fractional parts of whole objects or sets of <br> objects. | 3(3)(E) Number and operations. The <br> student applies mathematical process <br> standards to represent and explain fractional <br> units. |
| The student is expected to use fraction <br> names and symbols to describe fractional <br> parts of whole objects or sets of objects. | The student is expected to solve <br> problems involving partitioning an object <br> or a set of objects among two or more <br> recipients using pictorial representations <br> of fractions with denominators of $\mathbf{2 , 3}, \mathbf{4}$ <br> $\mathbf{6 , ~ a n d ~ 8 . ~}$ |

3(2)(D) Number, operation, and quantitative reasoning. The student uses fraction names and symbols (with denominators of 12 or less) to describe

+ fractional parts of whole objects or sets of objects.

The student is expected to construct concrete models of equivalent fractions for fractional parts of whole objects.

3(3)(F) Number and operations.The student applies mathematical process standards to represent and explain fractional units.

The student is expected to represent equivalent fractions with denominators of $2,3,4,6$, and 8 using a variety of objects and pictorial models, including number lines.

## Supporting Information

The current SE was separated into three revised SEs. Revised SE 3(3)(E) focuses on solving problems with fractional parts of whole objects or sets of objects.

Fractions should have denominators of 2,3 , 4,6 , or 8.

A fraction may be a part of a whole object or part of a set of objects.

Examples of problems include situations such as 2 children sharing 5 cookies.

Specificity has been added for the fractions that students are expected to model.
Fractions are greater than zero and less than or equal to one. The denominators may be 2 , $3,4,6$, or 8 . Objects, also called concrete models, that are linear in nature build to the use of strip diagrams as a pictorial model and number lines.

The revised SE includes the use of pictorial models, such as strip diagrams, and number lines.

Specificity has been added about the types of problems with the description of one- and two-step problems

3(5)(A) Algebraic reasoning. The student applies mathematical process standards to analyze and create patterns and relationships.

The student is expected to represent one- and two-step problems involving addition and subtraction of whole numbers to 1,000 using pictorial models number lines, and equations

Specificity has been added to the numbers contained within the problems as "whole numbers to 1,000 ."

Pictorial models should build to the use of number lines, such as a strip diagram.

The revised SE includes the use of numbe lines and equations to represent the problems.

## Grade 3 - Mathematics

|  | Old TEKS: Number, Operation, and Quantitatifve Reasoning | Current TEKS (2012) | Supporting I nformation | Notes |
| :---: | :---: | :---: | :---: | :---: |
| $3(3)(B)$ Number, operation, and quantitative reasoning. The student adds and subtracts to solve meaningful problems involving whole numbers. <br> The student is expected to select addition or subtraction and use the operation to solve problems involving whole numbers through 999. |  | 3(4)(A) Number and operations.The student applies mathematical process standards to develop and use strategies and methods for whole number computations in order to solve problems with efficiency and accuracy. <br> The student is expected to solve with fluency one-step and two-step problems involving addition and subtraction within 1,000 using strategies based on place value, properties of operations, and the relationship between addition and subtraction. | Specificity has been added about the types of problems with the description of one- and two-step problems. <br> Specificity continues with the numbers contained within the problems as "whole numbers within 1,000 ." |  |
|  |  | The revised SE includes specific approaches to solving the one-step and two-step problems: strategies based on place value, properties of operations, and the relationship between addition and subtraction. |  |
|  |  | add numbers such as 237 and 547. If using strategies based on place value, a student might add the hundreds to get 700, the tens to get 70, and the ones to get 14 and then combine 700,70 , and 14 to have a sum of 784. If using a strategy based on properties of operations, a student may consider that $237+547$ is equivalent to $237+(500+47)=$ $(237+500)+47=737+47=784$. If using a strategy based on the relationship between addition and subtraction, a student might subtract 63 from 547 and add it to 237 to have 300 and 484 which add to give 784 . <br> The revised SE includes fluency. |  |
| $\bullet+$ | 3(4)(A) Number, operation, and quantitative reasoning. The student recognizes and solves problems in multiplication and division situations. <br> The student is expected to learn and apply multiplication facts through 12 by 12 using concrete models and objects. |  | 3(4)(D) Number and operations. The student applies mathematical process standards to develop and use strategies and methods for whole number computations in order to solve problems with efficiency and accuracy. | Specificity has been added for the use of concrete models and objects. Arrays should reflect the combination of equally-sized groups of objects. |  |
|  |  |  | The student is expected to determine the total number of objects when equallysized groups of objects are combined or arranged in arrays up to $\mathbf{1 0}$ by 10. | The learning of facts related to 11 s and 12 s is not included in the Revised TEKS (2012). |  |
|  |  | 3(4)(E) Number and operations.The student applies mathematical process standards to develop and use strategies and methods for whole number computations in order to solve problems with efficiency and accuracy. | Specificity has been added about strategies that support the learning of multiplication facts: repeated addition, equal-sized groups, arrays, area models, equal jumps on a number line, and skip counting. |  |
|  |  | The student is expected to represent multiplication facts by using a variety of approaches such as repeated addition, equal-sized groups, arrays, area models, equal jumps on a number line, and skip counting. | The learning of facts related to 11 s and 12 s is not included in the Revised TEKS (2012). |  |

## Grade 3 - Mathematics



## Grade 3 - Mathematics

| Old TEKS: Number, Operation, and <br> Quantitatifue Reasoning |
| :--- |
|  |
| 3(4)(C) Number, operation, and |
| quantitative reasoning. The student |
| recognizes and solves problems in |
| multiplication and division situations. |
| The student is expected to use models to <br> solve division problems and use number | solve division problems and use number sentences to record the solutions.

## Current TEKS (2012)

3(4)(H) Number and operations.Th student applies mathematical process standards to develop and use strategies and methods for whole number computations in order to solve problems with efficiency and accuracy.

The student is expected to determine the number of objects in each group when a set of objects is partitioned into equal shares or a set of objects is shared equally.

3(4)(K) Number and operations. The $3(4)(K)$ Number and operations.The
student applies mathematical process standards to develop and use strategies and methods for whole number computations in order to solve problems with efficiency and accuracy.

The student is expected to solve onestep and two-step problems involving multiplication and division within 100 using strategies based on objects; pictorial models, including arrays, area models, and equal groups; properties of operations; or recall of facts.

Supporting I nformation Notes
Specificity has been added on how to use models to solve division problems.

Students are expected to think with both forms of division: partitioning into equal shares (determining the number of groups with a given number of objects in each group) and sharing equally (determining the number of items in each group when the objects are shared equally among a given number)

When paired with revised SEs 3(1)(D) and
3(1)(E), students may be asked to use
number sentences to record the solutions
The Revised SE 3(4)(K) builds to the Revised SE $3(5)(B)$. The focus of $3(4)(K)$ is on developing number-based strategies to solve multiplication and division problems within 100.

The use of models in the current SE includes the use of objects.
With revised SE 3(4)(K), the dividend must be less than 100.

Strategies to solve division problems other than concrete models, or objects, are included: pictorial models, including arrays, area models, and equal groups; properties, operations: and recall of facts.

## 3(5)(A) Number, operation and

 quantitative reasoning. The student estimates to determine reasonable results.The student is expected to round whole numbers to the nearest ten or hundred to approximate reasonable results in problem situations.
3(5)(B) Number, operation and quantitative reasoning. The student estimates to determine reasonable results.

The student is expected to use strategies including rounding and compatible numbers to estimate solutions to addition and subtraction problems.

3(4)(B) Number and operations.The
student applies mathematical process standards to develop and use strategies and methods for whole number computations in order to solve problems with efficiency and accuracy.

The student is expected to round to the nearest 10 or $\mathbf{1 0 0}$ or use compatible numbers to estimate solutions to addition and subtraction problems.

The current SEs 3(5)(A) and 3(5)B have been combined to form the revised SE 3(4)(B).

| Old TEKS: Number, Operation, and Quantitatifve Reasoning | Current TEKS (2012) | Supporting I nformation | Notes |
| :---: | :---: | :---: | :---: |
| $+$ | 3(2)(B) Number and operations.The student applies mathematical process standards to represent and compare whole numbers and understand relationships related to place value. <br> The student is expected to describe the mathematical relationships found in the base- 10 place value system through the hundred thousands place. | The mathematical relationships include interpreting the value of each place-value position as ten times the position to the right. <br> The revised SE 3(2)(B) builds to the revised SE 4(2)(A). |  |
| $\ddagger$ | 3(2)(C) Number and operations.The student applies mathematical process standards to represent and compare whole numbers and understand relationships related to place value. <br> The student is expected to represent a number on a number line as being between two consecutive multiples of 10 , $100,1,000$, or 10,000 and use words to describe relative size of numbers in order to round whole numbers. | This builds on number line understandings from grade 2 with Revised SEs 2(2)(E) and 2(2)(F). <br> Words may include phrases such as "closer to," "is about," or "is nearly." |  |
| $\uparrow$ | 3(3)(G) Number and operations.The student applies mathematical process standards to represent and explain fractional units. <br> The student is expected to explain that two fractions are equivalent if and only if they are both represented by the same point on the number line or represent the same portion of a same size whole for an area model. | The emphasis with this revised SE is on the understanding that equivalent fractions must be describing the same whole. $6 / 8$ does not equal $3 / 4$ when the $6 / 8$ is part of a candy bar and the $3 / 4$ is part of a pizza. While they both describe $3 / 4$ of their respective wholes, the amounts described by $6 / 8$ and $3 / 4$ are not the same. |  |
| $+$ | 3(4)(1) Number and operations.The student applies mathematical process standards to develop and use strategies and methods for whole number computations in order to solve problems with efficiency and accuracy. <br> The student is expected to determine if a number is even or odd using divisibility rules. | To determine if a number is even, one may apply the divisibility rule for 2: A number is divisible by 2 if the ones digit is even ( $0,2,4$, 6 , or 8 ). |  |

Grade 3 - Mathematics
Old TEKS: Patterns, Relationships,
and Algebraic Thinking
Current TEKS (2012)
Supporting Information
Notes

3(6) (A) Patterns, relationships, and algebraic thinking. The student uses patterns to solve problems

- The student is expected to identify and extend whole-number and geometric patterns to make predictions and solve problems.

3(6)(B) Patterns, relationships, and algebraic thinking. The student uses patterns to solve problems

The student is expected to identify patterns in multiplication facts using concrete objects, pictorial models, or technology.

3(4)(E) Number and operations.The
student applies mathematical process standards to develop and use strategies and methods for whole number computations in order to solve problems with efficiency and accuracy.

The student is expected to represent multiplication facts by using a variety of multipication facts by using a variety approaches such as repeated addition,
equal-sized groups, arrays, area models, equal-sized groups, arrays, area modeis,
equal jumps on a number line, and skip counting.

This skill is not included explicitly within the Revised TEKS (2012)

## 3(4)(J) Number and operations. The

student applies mathematical process standards to develop and use strategies and methods for whole number computations in order to solve problems with efficiency and accuracy.

The student is expected to determine a quotient using the relationship between
algebraic thinking. The student uses patterns to solve problems

+ The student is expected to identify patterns in related multiplication and division sentences (fact families) such as $2 \times 3=6,3 \times 2=6,6 \div 2=3,6 \div 3=2$.
multiplication and division.

3(5)(D) Algebraic reasoning. The student applies mathematical process standards to analyze and create patterns and relationships.

The student is expected to determine the unknown whole number in a multiplication or division equation relating three whole numbers when the unknown is either a missing factor or product.

Specificity for patterns in multiplication facts has been added with repeated addition, equal-sized groups, arrays, area models, equal jumps on a number line, and skip counting.

The identification of the relationship betwee multiplication and division, as seen in fact families, lays the foundation for determining a quotient based on this relationship.

Specificity has been added to identify the purpose of the relationship between multiplication and division to determining a quotient.

For example, the quotient of $40 \div 8$ can be found by determining what factor makes 40 when multiplied by 8 .

If the multiplication or division equation relates whole numbers from fact families up to $10 \times 10$, students may apply their knowledge of facts and the relationship between multiplication and division to determine the unknown number.

Students may be expected to use the relationship between multiplication and division for a problem such as $12=[] \div 6$. The student knows that if $12=[] \div 6$ then $12 \times 6=[]$ so []$=72$. Students may also be expected to solve problems where they state that the value 4 makes $3 \times[]=12$ a true equation.

Grade 3 - Mathematics

Old TEKS: Patterns, Relationships,
and Algebraic Thinking

3(7)(A) Patterns, relationships, and algebraic thinking. The student uses lists, tables, and charts to express patterns and relationships.

The student is expected to generate a table of paired numbers based on a reallife situation such as insects and legs.

3(7)(B) Patterns, relationships, and algebraic thinking. The student uses lists, tables, and charts to express patterns and relationships.

The student is expected to identify and describe patterns in a table of related number pairs based on a meaningfu problem and extend the table.
(5)(E) Algebraic reasoning. The studen applies mathematical process standards to analyze and create patterns and relationships.

The student is expected to represent real-world relationships using number pairs in a table and verbal descriptions

## Supporting Information

Notes
When paired with revised SE 3(1)(A), the expectation is that students apply this skill in a problem arising in everyday life, society, and the workplace.

When paired with revised SE 3(1)(D), the expectation is that students extend the relationship represented in a table to explore and communicate the implications of the relationship.

The revised SE restates "generate" as
"represent," a more appropriate verb to use when multiple representations such as table are used to represent a real-world
relationship. It also restates "identify and describe patterns in a table" with "represent real-world relationships using . . . verbal descriptions."

The revised SE 3(5)(E) builds to the revised SE 4(5)(B).

Real-world relationships include situations such as the following: 1 insect has 6 legs, 2 insects have 12 legs, and so forth.

The Revised SE 3(5)(B) is an extension of the Revised SE $3(4)(K)$. The focus of $3(5)(B)$ is on developing representations that build to numeric equations for multiplication and division situations by connecting arrays to strip diagrams.

With the current SEs related to multiplication, discussions have focused on multiplication as repeated addition, so $3 \times 24$ is often described as 3 groups of 24

With the revised SE, students also focus on the numerical relationship between 24 and the product $3 \times 24$. The product of $3 \times 24$ will be 3 times as much as 24 . This lays the foundation for future work in grade 5 with fraction multiplication and determining part of a number.

## Grade 3 - Mathematics

| Old TEKS: Geometry and Spatial <br> Reasoning | Current TEKS (2012) | Supporting Information |
| :--- | :--- | :--- |

## Grade 3 - Mathematics

| Old TEKS: Geometry and Spatial Reasoning | Current TEKS (2012) | Supporting I nformation | Notes |
| :---: | :---: | :---: | :---: |
|  | 3(3)(B) Number and operations.The student applies mathematical process standards to represent and explain fractional units. | Specificity has been added: the fractions for a specified point on a number line may be thirds, sixths, and eighths in addition to halves and fourths. |  |
| 3(10) Geometry and spatial reasoning. The student recognizes that a line can be used to represent numbers and fractions and their properties and relationships. | The student is expected to determine the corresponding fraction greater than zero and less than or equal to one with denominators of $2,3,4,6$, and 8 given a specified point on a number line. | The focus of the Revised SE 3(3)(B) is on the part to whole representations using tick marks on a number line. |  |
| The student is expected to locate and name points on a number line using whole numbers and fractions, including halves and fourths. | 3(7)(A) Geometry and measurement.The student applies mathematical process standards to select appropriate units, strategies, and tools to solve problems involving customary and metric measurement. <br> The student is expected to represent fractions of halves, fourths, and eighths as distances from zero on a number line. | The focus of the Revised $\operatorname{SE} 3(7)(A)$ is on the length of the portion of a number between 0 and the location of the point. <br> The Revised SE 3(7)(A) builds to the Revised SE 4(3)(G) where any fraction or decimals to tenths or hundredths may be represented as distances from zero on a number line. |  |

Grade 3 - Mathematics

3(11)(A) Measurement. The student directly compares the attributes of length, area, weight/mass, and capacity, and use comparative language to solve problems and answer questions. The student selects and

- uses standard units to describe length, area capacity/volume, and weight/mass.

The student is expected to use linear measurement tools to estimate and measure lengths using standard units.

3(11)(B) Measurement. The student directly compares the attributes of length, area, weight/mass, and capacity, and use comparative language to solve problems and
$+\quad$ answer questions. The student selects and uses standard units to describe length, area, capacity/volume, and weight/mass.

The student is expected to use standard units to find perimeter of a shape.

3(7)(B) Geometry and measurement.The student applies mathematical process standards to select appropriate units, strategies, and tools to solve problems involving customary and metric measurement.

The student is expected to determine the perimeter of a polygon or a missing ength when given perimeter and remaining side lengths in problems.

3(11)(C) Measurement. The student directly compares the attributes of length, area, weight/mass, and capacity, and use comparative language to solve problems and answer questions. The student selects and uses standard units to describe length, area, capacity/volume, and weight/mass.

The student is expected to use concrete and pictorial models of square units to determine the area of two-dimensional surfaces.

3(6)(C) Geometry and measurement.The student applies mathematical process standards to analyze attributes of twodimensional geometric figures to develop generalizations about their properties.

The student is expected to determine the area of rectangles with whole number side lengths in problems using multiplication related to the number of rows times the number of unit squares in each row.

This skill is not included explicitly within the Revised TEKS (2012)

This SE is subsumed within revised SE 3(1)(C) as linear measurement tools may be among the tools that students select to solve problems.

Students may measure the side lengths of a polygon to determine its perimeter using inches or centimeters. Side lengths should be whole numbers.

Students may be expected to determine a missing side length of a polygon when given the perimeter of the polygon and the remaining side lengths.

The revised SE limits the two-dimensional surfaces to rectangles with whole number side lengths.

Students may use concrete or pictorial models of square units to represent the number of rows and the number of unit squares in each row.

Units of area may be square inches or square centimeters
Students are expected to use multiplication to determine the area of a rectangle instead of counting squares.

With the revised SE, students are not expected to identify concrete models that approximate standard units of weight.

With the revised SE, students are not expected to determine mass.

Students are measuring weight.

Students are expected to use appropriate units and tools to determine weight in the customary system.

3(11)(D) Measurement. The student directly compares the attributes of length, area, weight/mass, and capacity, and use comparative language to solve problems and answer questions. The student selects and uses standard units to describe length, area, capacity/volume, and weight/mass.

The student is expected to identify concrete models that approximate standard units of weight/ mass and use them to measure weight/ mass.

3(7)(E) Geometry and measurement.The student applies mathematical process standards to select appropriate units, strategies, and tools to solve problems involving customary and metric measurement.

The student is expected to determine liquid volume (capacity) or weight using appropriate units and tools.

## Grade 3 - Mathematics



Grade 3 - Mathematics

| Old TEKS: Measurement | Current TEKS (2012) | Supporting Information | Notes |
| :---: | :---: | :---: | :---: |
| $+$ | 3(6)(D) Geometry and measurement.The student applies mathematical process standards to analyze attributes of twodimensional geometric figures to develop generalizations about their properties. <br> The student is expected to decompose composite figures formed by rectangles into non-overlapping rectangles to determine the area of the original figure using the additive property of area. | Composite figures should be comprised of no more than three rectangles, including squares as special cases of rectangles. |  |
| $\pm$ | 3(6)(E) Geometry and measurement.The student applies mathematical process standards to analyze attributes of twodimensional geometric figures to develop generalizations about their properties. <br> The student is expected to decompose two congruent two-dimensional figures into parts with equal areas and express the area of each part as a unit fraction of the whole and recognize that equal shares of identical wholes need not have the same shape. | Students may be expected to separate two congruent squares in half in two different ways. <br> Students may be expected to identify that the smaller parts represent one-half of each of the original squares even though the halves from one square are not congruent to the halves in the other square. |  |
| $\pm$ | 3(7)(D) Geometry and measurement. The student applies mathematical process standards to select appropriate units, strategies, and tools to solve problems involving customary and metric measurement. <br> The student is expected to determine when it is appropriate to use measurements of liquid volume (capacity) or weight. | Students are expected to distinguish between liquid ounces and ounces that measure weight. |  |

## Grade 3 - Mathematics

3(13)(A) Probability and statistics. The student solves problems by collecting, organizing, displaying, and interpreting sets of data.
The student is expected to collect, organize, record, and display data in pictographs and bar graphs where each picture or cell might represent more than one piece of data.

3(8)(A) Data analysis. The student applies mathematical process standards to solve problems by collecting, organizing, displaying and interpreting data.

The student is expected to summarize a data set with multiple categories using a frequency table, dot plot, pictograph, or bar graph with scaled intervals.

3(13)(B) Probability and statistics. The student solves problems by collecting, organizing, displaying, and interpreting sets of data.

The student is expected to interpret information from pictographs and bar graphs.

3(8)(B) Data analysis. The student applie mathematical process standards to solve problems by collecting, organizing, displaying, and interpreting data.

The student is expected to solve oneand two-step problems using categorical data represented with a frequency table, dot plot, pictograph, or bar graph with scaled intervals.

The phrase "where each picture or cell might represent more than one piece of data" has been restated as "with scaled intervals."

A frequency table shows how often an item, a number, or a range of numbers occurs. Tallies and counts are used to record frequencies. Students begin work with frequency tables in grade 3.

A dot plot may be used to represent
frequencies. A number line may be used for counts related to numbers. A line labeled with categories may be used as well if the context requires. Dots are recorded vertically above the number line to indicate frequencies. Dots may represent one count or multiple counts if so noted. Students begin work with dot plots in grade 3.
Students begin work with pictographs in grade K and bar graphs in grade 1 with the Revised TEKS (2012)

Specificity for the purpose of interpreting graphs has been added with the phrase "solve one- and two-step problems."

Specificity has been added regarding the type of data. Categorical data are the focus in grade 3

Specificity regarding the graphical
representations has been added with the phrase "with scaled intervals."

Students begin work with frequency tables and dot plots in grade 3 with the Revised TEKS (2012).

## 3(13)(C) Probability and statistics. The

student solves problems by collecting,
organizing, displaying, and interpreting sets of data.

The student is expected to use data to
describe events as more likely than, less likely than, or equally likely as.

## Grade 3 - Mathematics

Old TEKS: Underlying Processes and Mathematical Tools

Current TEKS (2012)
Supporting Information
Notes
$3(14)(A)$ Underlying processes and mathematical tools. The student applies Grade 3 mathematics to solve problems connected to everyday experiences and activities in and outside of school.

The student is expected to identify the mathematics in everyday situations.

3(1)(A) Mathematical process standards. The student uses mathematical processes to acquire and demonstrate mathematical understanding.

The student is expected to apply mathematics to problems arising in everyday life, society, and the workplace.

The focus has shifted to application
The opportunities for application have been consolidated into three areas: everyday life, society, and the workplace.

This SE, when tagged to a content SE, allows for increased rigor through connections outside the discipline.

3(14)(B) Underlying processes and mathematical tools. The student applies Grade 3 mathematics to solve problems connected to everyday experiences and activities in and outside of school.

The student is expected to solve problems that incorporate understanding the problem, making a plan, carrying out the plan, and evaluating the solution for reasonableness.

3(14)(C) Underlying processes and mathematical tools. The student applies Grade 3 mathematics to solve problems connected to everyday experiences and activities in and outside of school.

The student is expected to select or develop an appropriate problem-solving plan or strategy including drawing a picture, looking for a pattern, systematic guessing and checking, acting it out, making a table, working a simpler problem, or working backwards to solve a problem.

3(14)(D) Underlying processes and mathematical tools. The student applies Grade 3 mathematics to solve problems connected to everyday experiences and activities in and outside of school.

The student is expected to use tools such as real objects, manipulatives, and technology to solve problems.

3(1)(C) Mathematical process standards. The student uses mathematical processes to acquire and demonstrate mathematical understanding.

The student is expected to select tools, including real objects, manipulatives, paper and pencil, and technology as appropriate, and techniques, including mental math, estimation, and number sense as appropriate, to solve problems.

The revised SE restates and condenses 3(14)(B) and 3(14)(C).

| Problem-Solving Model |  |
| :--- | :--- |
| Current TEKS | Revised TEKS <br> (2012) |
| Understanding the <br> problem | Analyzing given <br> information |
| Making a plan | Formulating a <br> plan or strategy |
| Carrying out the <br> plan | Determining a <br> solution |
|  | Justifying the <br> solution |
| Evaluating the | Evaluating the <br> problem-solving <br> process and the <br> reasonableness <br> of the solution |
| reasonableness |  |

The phrase "as appropriate" has been inserted into the Revised TEKS (2012). This implies that students are assessing which tool to apply rather than trying only one or all.
"Paper and pencil" is now included in the list of tools that still includes real objects, manipulatives, and technology.

| Grade 3 - Mathematics |  |  |  |
| :---: | :---: | :---: | :---: |
| OId TEKS: Underlying Processes and Mathematical Tools | Current TEKS (2012) | Supporting I nformation | Notes |
| 3(15)(A) Underlying processes and mathematical tools. The student communicates about Grade 3 mathematics using informal language. <br> The student is expected to explain and record observations using objects, words, pictures, numbers, and technology. | 3(1)(D) Mathematical process standards. The student uses mathematical processes to acquire and demonstrate mathematical understanding. <br> The student is expected to communicate mathematical ideas, reasoning, and their implications using multiple representations, including symbols, diagrams, graphs, and language as appropriate. | Communication has expanded to include "reasoning" and the implications of mathematical ideas and reasoning. <br> The list of representations is now summarized with "multiple representations" with specificity added for symbols and diagrams. |  |
| 3(15)(B) Underlying processes and mathematical tools. The student communicates about Grade 3 mathematics using informal language. <br> The student is expected to relate informal language to mathematical language and symbols. | 3(1)(E) Mathematical process standards. The student uses mathematical processes to acquire and demonstrate mathematical understanding. <br> The student is expected to create and use representations to organize, record, and communicate mathematical ideas. | The use of representations is extended to include organizing and recording mathematical ideas in addition to communicating. <br> As students use and create representations, it is implied that they will evaluate the effectiveness of their representations to ensure that they are communicating mathematical ideas clearly. <br> Students are expected to use appropriate mathematical vocabulary and phrasing when communicating mathematical ideas. |  |
| 3(16)(A) Underlying processes and mathematical tools. The student uses logical reasoning. <br> The student is expected to make generalizations from patterns or sets of examples and nonexamples. | 3(1)(F) Mathematical process standards. The student uses mathematical processes to acquire and demonstrate mathematical understanding. <br> The student is expected to analyze mathematical relationships to connect and communicate mathematical ideas. | The Revised TEKS (2012) extends the current TEKS to allow for additional means to analyze relationships and to form connections with mathematical ideas past conjecturing and sets of examples and non-examples. <br> Students are expected to form conjectures based on patterns or sets of examples and non-examples. |  |
| 3(16)(B) Underlying processes and mathematical tools. The student uses logical reasoning. <br> The student is expected to justify why an answer is reasonable and explain the solution process. | 3(1)(G) Mathematical process standards. The student uses mathematical processes to acquire and demonstrate mathematical understanding. <br> The student is expected to display, explain, and justify mathematical ideas and arguments using precise mathematical language in written or oral communication. | The Revised TEKS (2012) clarifies "validates his/her conclusions" with displays, explanations, and justifications. The conclusions should focus on mathematical ideas and arguments. <br> Displays could include diagrams, visual aids, written work, etc. The intention is make one's work visible to others so that explanations and justifications may be shared in written or oral form. <br> Precise mathematical language is expected. For example, students would use "vertex" instead of "corner" when referring to the point at which two edges intersect on a polygon. |  |


| Old TEKS: Financial Literacy | Current TEKS (2012) | Supporting Information | Notes |
| :---: | :---: | :---: | :---: |
| $+$ | 3(9)(A) Personal financial literacy. <br> The student applies mathematical process standards to manage one's financial resources effectively for lifetime financial security. <br> The student is expected to explain the connection between human capital/ labor and income. |  |  |
| $+$ | 3(9)(B) Personal financial literacy. The student applies mathematical process standards to manage one's financial resources effectively for lifetime financial security. <br> The student is expected to describe the relationship between the availability or scarcity of resources and how that impacts cost. |  |  |
| $+$ | 3(9)(C) Personal financial literacy. <br> The student applies mathematical process standards to manage one's financial resources effectively for lifetime financial security. <br> The student is expected to identify the cost and benefits of planned and unplanned spending decisions. |  |  |
| $+$ | 3(9)(D) Personal financial literacy. <br> The student applies mathematical process standards to manage one's financial resources effectively for lifetime financial security. <br> The student is expected to explain that credit is used when wants or needs exceed the ability to pay and that it is the borrower's responsibility to pay it back to the lender, usually with interest. |  |  |
| $+$ | 3(9)(E) Personal financial literacy. <br> The student applies mathematical process standards to manage one's financial resources effectively for lifetime financial security. <br> The student is expected to list reasons to save and explain the benefit of a savings plan, including for college. |  |  |
| $+$ | 3(9)(F) Personal financial literacy. The student applies mathematical process standards to manage one's financial resources effectively for lifetime financial security. <br> The student is expected to identify decisions involving income, spending, saving, credit, and charitable giving. |  |  |

